

# IMPLEMENTATIONS OF AES ALGORITHM FOR REDUCING HARDWARE WITH IMPROVED EFFICIENCY

## Background of the Invention

### 5    1. Field of the Invention

The present invention is generally related to apparatus and method for implementing encryption and decryption using the AES (advanced encryption standard) algorithm, more particularly, 10 to a technique for reducing hardware used for encrypting and decrypting using the AES algorithm.

### 2. Description of the Related Art

Inexpensive high-speed Internet access 15 technologies, including optical fiber networks, ADSL (asymmetric digital subscriber line) networks, and cable television networks and so on, promote use of VPN (virtual private network) technologies, which provide secure communications 20 through public communication networks. The use of VPN eliminates the necessity of expensive private links, and preferably reduces communications cost.

Typical VPN technologies adopt the US government's data encryption standard (DES) 25 algorithm, which uses 56-bit common keys, or the Triple-DES algorithm, which uses three passes of the DES algorithms. Nevertheless, these

algorithms do not satisfy recent requirements; the DES seems to be no longer sufficient to provide the necessary security, while the Triple-DES requires a large amount of processing.

5           The AES algorithm, which is based on the Rijndael algorithm, is a promising candidate of the next-generation encryption algorithm for VPN. The security of the AES algorithm is at least as good as the Triple-DES, and superior to it in  
10 efficiency. This situation necessitates encryption and decryption platforms adapted to the AES algorithm, including AES-dedicated hardware and software.

          Federal Information Processing Standards  
15 Publication 197, hereinafter referred to as FIPS 197, the entire disclosure of which is incorporated herein by reference, presents the procedure of implementing the AES algorithm.

          The input for the AES algorithm consists of  
20 sequences of 128 bits, which are referred to as blocks. The AES algorithm divides the 128-bit input into 16 bytes (each consisting of 8 bits), and arranges the 16 bytes to generate a two-dimensional array of bytes called the state. The  
25 state consists of four rows and four columns of bytes. The AES algorithm's operations are performed on states. The input, which is the

array of bites  $in_0, in_1 \dots in_{15}$ , is copied into the state Array as illustrated in Fig. 1. The  $(i, j)$  element of the state is denoted by  $S_{i,j}$  for  $0 \leq i, j \leq 3$ , hereinafter.

5           Fig. 2 is a flowchart illustrating the encrypting procedure using the AES algorithm, which is described in the pseudo code in FIPS 197.

For encryption, the AES algorithm involves repeatedly implementing a set of transformations  
10 called "round". The number of the rounds, which is denoted by  $Nr$ , depends on the key lengths. The numbers of rounds for the key lengths of 128, 192, and 256 are 10, 12, and 14, respectively.

Each round is composed of four  
15 transformations called "SubBytes", "ShiftRows", "MixColumns", and "AddRoundKey", which are denoted by numerals 1404, 1405, 1406, and 1407, respectively, with exception of the final round 1408, which does not include the MixColumns  
20 transformation.

Encryption using the AES algorithm begins with an initial AddRoundKey transformation 1402. After the initial AddRoundKey transformation 1402, the first  $Nr-1$  rounds 1403 are implemented  
25 repeatedly, which is followed by the final round 1408.

The following is a brief explanation of the

• aforementioned four transformations "SubBytes",  
"ShiftRows", "MixColumns", and "AddRoundKey".  
Details of these transformations are given in  
FIPS 197.

5           The SubBytes transformation 1404 is a byte  
substitution on each byte of the state using a  
substitution table called "S-Box". The S-Box,  
whose contents are disclosed in Figure 7 of FIPS  
197, is constructed by composing two  
10 transformations: taking the multiplicative  
inverse in the Galois field  $GF(2^8)$ , and applying  
an affine transformation over the  $GF(2^8)$ .

          In the ShiftRows transformation 1405, the  
bytes of the last three rows of the state are  
15 shifted over different numbers of bytes.

          The MixColumns transformation 1406 operates  
on the state column-by-column, treating each  
column as a four-term polynomial. The columns are  
considered as polynomials over  $GF(2^8)$  and  
20 multiplied with a fixed polynomial.

          In the AddRoundKey transformation, a Round  
Key, which is generated through a key expansion  
of a common key, is added to the state by a  
simple bitwise XOR operation.

25           It should be noted that addition and  
multiplication in the MixColumns and AddRoundKey  
transformations are implemented over the Galois

field  $GF(2^8)$ . Adders for implementing addition over  $GF(2^8)$ , which computes the sum of two GF elements by XORing the corresponding bits, only requires reduced hardware typically including  
5 several logic gates. In contrast, multipliers for implementing multiplication over  $GF(2^8)$  requires increased hardware, typically including several tens of logic gates.

The SubBytes, ShiftRows, and MixColumns  
10 transformations 1404, 1405, and 1406, which are the components of the round, are often performed collectively to improve the throughput. There is a need for providing a method for efficiently performing these transformations for improving  
15 efficiency because of the following reasons. The SubBytes and MixColumns transformations require a large amount of processing because the SubBytes transformation includes many table lookups, and the MixColumns transformation includes  
20 multiplication over the Galois field  $GF(2^8)$ . In addition, the ShiftRows and SubBytes transformations can be performed collectively, which desirably improves efficiency. It should be noted that the AddRoundKey transformation is  
25 usually performed independently, because of its high simplicity and independence.

Fig. 3 is a signal flow diagram

illustrating a conventional method of  
implementing the SubBytes, ShiftRows, and  
MixColumns transformations collectively for  
obtaining the first column of the transformation  
5 result, the first column including four elements.  
The first column of the transformation result is  
obtained from the state elements  $S_{0,0}$ ,  $S_{1,1}$ ,  $S_{2,2}$ ,  
and  $S_{3,3}$ .

Although Fig. 2 illustrates that a round  
10 begins with the SubBytes transformation, the  
method begins with the ShiftRows transformation.  
It should be noted that the SubBytes, and  
ShiftRows transformations commute, and thus the  
same result is obtained regardless of the order  
15 in which the SubBytes and ShiftRows  
transformations are performed.

The ShiftRows transformation is implemented  
by obtaining the associated elements using table  
lookups from the state. The MixColumns  
20 transformation is achieved by multiplication of  
the substitution values obtained from the S-box  
with corresponding coefficients followed by  
addition 1503, the coefficients being defined as  
disclosed in FIFP 197 (see formula (5.6)). In Fig.  
25 3, the multiplication over  $GF(2^8)$  in hexadecimal  
notation is denoted by symbols " $\cdot\{xy\}$ " where  $xy$  is  
a hexadecimal value.

The same goes for the reminder columns of the transformation result. The second column is obtained from the elements  $S_{0,1}$ ,  $S_{1,2}$ ,  $S_{2,3}$ , and  $S_{3,0}$ , the third column is obtained from the elements  
5  $S_{0,2}$ ,  $S_{1,3}$ ,  $S_{2,0}$ , and  $S_{3,1}$ , and the fourth column is obtained from the elements  $S_{0,3}$ ,  $S_{1,0}$ ,  $S_{2,1}$ , and  $S_{3,2}$ .

In order to improve the throughput, conventional hardware for implementing AES rounds is often provided with a plurality of S-boxes to  
10 perform parallel processing. For example, Seike et al. discloses a Rijndael processor performing parallel processing of all the 16 elements of the state using 16 S-Boxes having the same content in "Trial produce of the AES cryptography using  
15 FPGA," p.13, Technical Report of IEICE, VLD2001-91, ICD2001-136, PTS2001-38, November 2001. Schaumont et al. discloses a similar Rijndael processor having 16 S-Boxes in "Unlocking the design secrets of a 2.29 Gb/s Rijndael  
20 processor," Design Automation Conference, 2002. Proceedings. 39th, 2002, pp. 634-639.

McLoone et al. discloses a look-up table based Rijndael design to achieve an improved speed in Signal Processing Systems, 2001 IEEE  
25 Workshop on, 2001, pp. 349-360. The design implements not only the SubBytes transformation but also the ShiftRows and MixColumns

transformations as look-up tables (LUTs). Fig. 4 is a signal flow diagram illustrating the procedure of implementing the SubBytes, ShiftRows, and MixColumns transformations for the first 5 column of the transformation result. The design includes additional two further LUTs in place of the Galois field multipliers 1502; one containing the values of the SubBytes LUT multiplied in  $GF(2^8)$  by the hexadecimal number "02", the other 10 containing the values of the SubBytes LUT multiplied in  $GF(2^8)$  by the hexadecimal number "03". These additional LUTs are used to perform parallel processing.

The round of the AES algorithm may be 15 implemented by software. Gladman discloses a source code for implementing the AES algorithm in "Implementations of AES (Rijndael) in C/C++ and Assembler," [http://fp.gladman.plus.com/cryptography\\_technology/rijndael](http://fp.gladman.plus.com/cryptography_technology/rijndael).

20 Fig. 5 illustrates the Gladman's method for implementing the round for the AES algorithm. The method involves preparing "expanded" S-Boxes #0 to #3, which consist of 256 32-bit words, in a main memory. Each 32-bit word of the expanded S-Boxes #0 contains bits #0 to #31, wherein the 25 bits #0 to #7 contains the corresponding value of the SubBytes S-box multiplied by the hexadecimal



'number "02", the bits #8 to #15 contains the corresponding value of the SubBytes S-box multiplied by the hexadecimal number "01", the bits #16 to #23 contains the corresponding value  
5 of the SubBytes S-box multiplied by the hexadecimal number "01", and the bits #24 to #31 contains the corresponding value of the SubBytes S-box multiplied by the hexadecimal number "02". Correspondingly, each 32-bit word of the expanded  
10 S-Boxes #1 contains sequences of bits #0 to #7, #8 to #15, #16 to #23, and #24 to 31 which sequences respectively contain the corresponding values of the SubBytes S-box multiplied by the hexadecimal number "03", "02", "01", and "01",  
15 each 32-bit word of the expanded S-Boxes #2 contains sequences of bits #0 to #7, #8 to #15, #16 to #23, and #24 to 31 which sequences respectively contain the corresponding values of the SubBytes S-box multiplied by the hexadecimal  
20 number "01", "03", "02", and "01", and each 32-bit word of the expanded S-Boxes #3 contains sequences of bits #0 to #7, #8 to #15, #16 to #23, and #24 to 31 which sequences respectively contain the corresponding values of the SubBytes  
25 S-box multiplied by the hexadecimal number "01", "01", "03", and "02".

The "expanded" S-Boxes #0 to #3 enables

'SIMD (single instruction multiple data)  
processing for implementing the SubBytes,  
ShiftRows, and MixColumns transformations with  
reduced amount of processing, which only includes  
5 four table lookups to the expanded S-Boxes and  
four additions 1703 in  $GF(2^8)$ . This allows the  
Gladman's method to achieve an improved speed.

The aforementioned cipher transformations  
can be inverted and then implemented in reverse  
10 order to achieve description for the AES  
algorithm.

Fig. 6 is a flowchart of implementing  
decryption according to the AES algorithm. The  
decryption begins with an initial AddRoundKey  
15 transformation 1802. After the initial  
AddRoundKey transformation 1802, first to  $(Nr-1)$ -  
th rounds 1803 are implemented, and followed by a  
final round 1808. The rounds includes InvSubBytes,  
InvShiftRows, InvMixColumns, and AddRoundKey'  
20 transformations 1804, 1805, 1806, and 1807, with  
exception of the final round 1408, which does not  
include the MixColumns transformation, where the  
InvSubBytes, InvShiftRows, InvMixColumns, and  
AddRoundKey' transformations 1804, 1805, 1806,  
25 and 1807 are the inverses of the SubBytes,  
ShiftRows, MixColumns, and AddRoundKey  
transformations 1404, 1405, 1406, and 1407,

respectively. It should be noted that the AddRoundKey transformation is its inverse itself; however, the prime is attached to distinguish the inverse from the AddRoundKey transformation.

5           It should be noted that the inverse transformations are not implemented in the reverse order to the cipher transformations; the order of the inverse transformations are optimized to improve efficiency.

10           First, the InvShiftRows and InvSubBytes transformations 1805 and 1804 are permuted. This permutation is effective for improving the processing speed with the transformation result unchanged. It should be noted that the  
15   InvShiftRows and InvSubBytes transformations commute.

          Second, the AddRoundKey' and InvMixColumns transformations 1807, and 1806 are permuted. In the reverse order of the cipher transformation,  
20   the InvMixColumns transformation 1806 would operate on the result of the AddRoundKey' transformation 1807; however, the order is modified to improve efficiency. It should be noted that the permutation of the AddRoundKey'  
25   and InvMixColumns transformations requires that expanded keys going through the InvMixColumns transformations 1807 be used for the AddRoundKey'

transformation 1807 in place of the original expanded keys.

As illustrated in Fig. 4 and Fig. 6, rounds for AES-based encryption are almost similar to those for decryption; the difference are the contents of the S-boxes used for the SubBytes and InvSubBytes transformations 1404, and 1804, and the coefficients used for the MixColumns and InvMixColumns transformations 1406 and 1806. In the InvSubBytes transformations 1804, the inverse S-box, which is defined as illustrated in Figure 14 of FIPS 197, while the InvMixColumns transformations 1806 use the coefficients described in formula (5.10) of FIPS 197.

One of the drawbacks of the conventional encryption and decryption architectures is that it requires increased hardware for improving processing speed. The conventional architectures use a plurality of lookup tables to achieve parallel processing; however, the increase in the lookup tables causes an undesirable increase in hardware. Only a single S-box containing 256 8-bit words requires several thousands of logic gates.

Therefore, there is a need for providing apparatus and method for implementing the AES algorithm with reduced hardware and sufficient

throughput.

### 3. List of other Prior art documents

The following is a description of  
5 conventional Galois field processors; a m-bit  
multiplier module for multiplication over a  
Galois field  $GF(2^m)$  is disclosed in Japanese Open  
Laid Patent Application No. Jp-A 2002-23999.  
Galois field processors for computing the  
10 multiplicative inverse in  $GF(2^8)$  are disclosed in  
Japanese Open Laid Patent Applications No. Jp-A  
2000-322280A, and Jp-A-Heisei 11-249921. An error  
correction circuit including Galois field  
processors, each of which has a Galois field  
15 adder and multiplier, is disclosed in Japanese  
Open Laid Patent Application No. Jp-A-Showa 63-  
186338.

### **Summary of the Invention**

20 An object of the present invention is to  
provide a technology for implementing the AES  
algorithm with reduced hardware and sufficient  
throughput.

In an aspect of the present invention, an  
25 AES encryption processor is composed of a  
selector unit selecting an element of a state in  
response to row and column indices, a S-box for

obtaining a substitution value with the selected element used as an index, a coefficient table providing first to fourth coefficients in response to the row index, first to fourth Galois field multiplexers respectively computing first to fourth products, which are obtained by multiplication of the substitution value with first to fourth coefficients, respectively, and an accumulator which accumulates the first to fourth products to develop first to fourth elements of a designated column of a resultant state.

In an embodiment, the first to fourth coefficients are respectively set to {02}, {01}, {01}, and {03} in response to the row index selecting a first row of the state, to {03}, {02}, {01}, and {01} in response to the row index selecting a second row of the state, to {01}, {03}, {02}, and {01} in response to the row index selecting a third row of the state, and to {01}, {01}, {03}, and {02} in response to the row index selecting a fourth row of the state.

In another aspect of the present invention, an AES encryption processor is provided which is adapted to an AES instruction including first and second operands respectively selecting input and output registers out of a register file, and an

immediate operand selecting a row of a state. The  
AES encryption processor is composed of a  
selector unit selecting an element of the state  
in response to the first operand and the  
5 immediate operand, the selected element being  
stored in the input register, a S-box for  
obtaining a substitution value with the selected  
element used as an index, a coefficient table  
providing first to fourth coefficients in  
10 response to the immediate operand, first to  
fourth Galois field multiplexers respectively  
computing first to fourth products, which are  
obtained by multiplication of the substitution  
value with first to fourth coefficients,  
15 respectively, and a storing unit for storing the  
first to fourth products into the output register  
selected by the second operand.

The AES encryption processor preferably  
includes a processing unit adapted to implement  
20 XORing, when the AES encryption processor is  
further adapted to an XOR instruction; the  
processing unit implements XORing of values  
contained in two selected registers of the  
register file.

25 In still another aspect of the present  
invention, an AES decryption processor is  
composed of a selector unit selecting an element

of a state in response to row and column indices,  
an inverse S-box for obtaining a substitution  
value with the selected element used as an index,  
a coefficient table providing first to fourth  
5 coefficients in response to the row index, first  
to fourth Galois field multiplexers respectively  
computing first to fourth products, which are  
obtained by multiplication of the substitution  
value with first to fourth coefficients,  
10 respectively, and an accumulator which  
accumulates the first to fourth products to  
develop first to fourth elements of a designated  
column of a resultant state.

In still another aspect of a present  
15 invention, an AES decryption processor is  
provided which is adapted to an AES instruction  
including first and second operands respectively  
selecting input and output registers out of a  
register file, and an immediate operand selecting  
20 a row of a state. The AES decryption processor is  
composed of a selector unit selecting an element  
of the state in response to the first operand and  
the immediate operand, the selected element being  
stored in the input register, a S-box for  
25 obtaining a substitution value with the selected  
element used as an index, a coefficient table  
providing first to fourth coefficients in



response to the immediate operand, first to  
fourth Galois field multiplexers respectively  
computing first to fourth products, which are  
obtained by multiplication of the substitution  
5 value with first to fourth coefficients,  
respectively, and a storing unit for storing the  
first to fourth products into the output register  
selected by the second operand.

In still another aspect of the present  
10 invention, an AES processor adapted to both  
encryption and decryption is composed of a first  
selector unit selecting an element of a state in  
response to row and column indices, an inverse  
affine transformation circuit applying an inverse  
15 affine transformation on the selected element, a  
second selector unit selecting one out of two  
data bytes consisting of the selected element  
received from the first selector, and a result of  
the inverse affine transformation received the  
20 inverse affine transformation circuit, wherein  
the selected element is selected for encryption,  
while the result of the inverse affine  
transformation is selected for decryption, an  
inverse determining unit obtaining a  
25 multiplicative inverse of the selected data byte  
received from the second selector, an affine  
transformation circuit applying an affine

transformation on the obtained multiplicative  
inverse, a third selector unit selecting one of  
two data bytes consisting of the multiplicative  
inverse received from the inverse determining  
5 unit, and a result of the affine transformation  
received from affine transformation circuit,  
wherein the result of the affine transformation  
is selected for decryption, while the  
multiplicative inverse is selected for encryption,  
10 a coefficient table providing first to fourth  
coefficients in response to the row index, first  
to fourth Galois field multiplexers respectively  
computing first to fourth products, which are  
obtained by multiplication of the substitution  
15 value with first to fourth coefficients,  
respectively, and an accumulator which  
accumulates the first to fourth products to  
develop first to fourth elements of a designated  
column of a resultant state.

20 In still another aspect of the present  
invention, an AES processor is provided which is  
adapted to an AES instruction including first and  
second operands respectively selecting input and  
output registers out of a register file, and an  
25 immediate operand selecting a row of a state. The  
AES processor is composed of a first selector  
unit selecting an element of the state in

response the first operand and the immediate operand, the selected element being stored in the input register, an inverse affine transformation circuit applying an inverse affine transformation  
5 on the selected element, a second selector unit selecting one out of two data bytes consisting of the selected element received from the first selector, and a result of the inverse affine transformation received the inverse affine  
10 transformation circuit, wherein the selected element is selected for encryption, while the result of the inverse affine transformation is selected for decryption, an inverse determining unit obtaining a multiplicative inverse of the  
15 selected data byte received from the second selector, an affine transformation circuit applying an affine transformation on the obtained multiplicative inverse, a third selector unit selecting one of two data bytes consisting of the  
20 multiplicative inverse received from the inverse determining unit, and a result of the affine transformation received from affine transformation circuit, wherein the result of the affine transformation is selected for decryption,  
25 while the multiplicative inverse is selected for encryption, a coefficient table providing first to fourth coefficients in response to the row

index, first to fourth Galois field multiplexers respectively computing first to fourth products, which are obtained by multiplication of the substitution value with first to fourth  
5 coefficients, respectively, and a storing unit for storing the first to fourth products into the output register selected by the second operand.

In still another aspect of the present invention, an AES processor is provided which is  
10 adapted to an AES instruction including first and second operands respectively selecting input and output registers out of a register file, and an immediate operand selecting a row of a state(s). The AES processor is composed of a plurality of  
15 AES processor cores respectively associated with a plurality of columns of the state(s), a coefficient table providing first to fourth coefficients in response to the immediate operand. Each of the plurality of AES processor cores  
20 includes a first selector unit selecting an element of the state(s) in response the first operand and the immediate operand, the selected element being stored in the input register, an inverse affine transformation circuit applying an  
25 inverse affine transformation on the selected element, a second selector unit selecting one out of two data bytes consisting of the selected

element received from the first selector, and a  
result of the inverse affine transformation  
received the inverse affine transformation  
circuit, wherein the selected element is selected  
5 for encryption, while the result of the inverse  
affine transformation is selected for decryption,  
an inverse determining unit obtaining a  
multiplicative inverse of the selected data byte  
received from the second selector, an affine  
10 transformation circuit applying an affine  
transformation on the obtained multiplicative  
inverse, a third selector unit selecting one of  
two data bytes consisting of the multiplicative  
inverse received from the inverse determining  
15 unit, and a result of the affine transformation  
received from affine transformation circuit,  
wherein the result of the affine transformation  
is selected for decryption, while the  
multiplicative inverse is selected for encryption,  
20 first to fourth Galois field multiplexers  
respectively computing first to fourth products,  
which are obtained by multiplication of the  
substitution value with first to fourth  
coefficients, respectively, and a storing unit  
25 for storing the first to fourth products into the  
output register selected by the second operand.

### Brief Description of the Drawings

Fig. 1 illustrates the data structure of the state, which is used for implementing the AES algorithm;

5           Fig. 2 is a flowchart illustrating a typical procedure of implementing encryption using the AES algorithm;

Fig. 3 is a signal flow diagram illustrating a typical procedure of collectively  
10 implementing the SubBytes, ShiftRows, and MixColumns transformations;

Fig. 4 is a signal flow diagram illustrating the McLoone's method of collectively implementing the SubBytes, ShiftRows, and  
15 MixColumns transformations;

Fig. 5 is a signal flow diagram illustrating the Gladman's method of collectively implementing the SubBytes, ShiftRows, and MixColumns transformations;

20           Fig. 6 is a flowchart illustrating a typical procedure of implementing decryption using the AES algorithm;

Fig. 7 is a block diagram illustrating a structure of an AES encryption processor in a  
25 first embodiment;

Fig. 8 is a table illustrating values contained in a coefficient table used for

encryption;

Fig. 9 is a diagram illustrating the operation implemented by the AES encryption processor in the first embodiment;

5 Fig. 10 is a block diagram illustrating an AES encryption processor in a second embodiment;

Figs. 11A and 11B illustrates data structure of input and output registers, respectively;

10 Fig. 12 is a table illustrating the result of an AES\_SSM instruction, which depends on the immediate operand thereof;

Fig. 13 is an instruction code using AES\_SSM instructions for achieving the SubBytes, ShiftRows, and MixColumns transformations;

15 Fig. 14 is a table illustrating values contained in a coefficient table used for decryption;

Fig. 15 is a table illustrating the result of an inverse AES\_SSM instruction, which depends on the immediate operand thereof;

Fig. 16 is a block diagram illustrating a structure of an AES encryption/decryption processor in a third embodiment;

25 Fig. 17 is a block diagram illustrating a structure of an AES processor in a fourth embodiment;

Fig. 18 is a circuit diagram of a typical adder for achieving the addition in  $GF(2^8)$ ;

Fig. 19 is a circuit diagram of a typical multiplier for achieving the multiplication of an element with a hexadecimal value {02} in  $GF(2^8)$ ;

Fig. 20 is a circuit diagram of a typical multiplier for achieving the multiplication in  $GF(2^8)$ ;

Fig. 21 is a table illustrating the values contained in the S-box used for the SubBytes transformation;

Fig. 22 is a table illustrating the values contained in the inverse S-box used for the InvSubBytes transformation; and

Fig. 23 is a table illustrating the values contained in an inverse table used for taking a multiplicative inverse in  $GF(2^8)$ .

#### **Description of the Preferred Embodiments**

Preferred embodiments of the present invention are described below in detail with reference to the attached drawings. In the drawings, like or similar elements are designated by identical reference numerals throughout the several views thereof.

#### 1. Operations over Galois field $GF(2^8)$



As described in FIPS 197, the AES algorithm involves various operations over Galois field  $GF(2^8)$ . The following is a brief description of the Galois field operations.

5

#### 1-1) Element in $GF(2^8)$

The Galois field  $GF(p^m)$  can be generated as the set of polynomials with coefficients in  $GF(2)$  modulo an irreducible polynomial of degree  $m$ . A polynomial  $b(x)$  that is an element in  $GF(2^8)$  is described as follows:

$$b(x) = b_7x^7 + b_6x^6 + b_5x^5 + b_4x^4 + b_3x^3 + b_2x^2 + b_1x^1 + b_0, \dots(1)$$

where  $b_i$  is the selected value out of 1 and 0, which are the elements in  $GF(2)$ , for  $0 \leq i \leq 7$ . In binary notation, this polynomial is described as  $\{b_7b_6b_5b_4b_3b_2b_1b_0\}$ . Elements in  $GF(2^8)$  may be expressed in hexadecimal notation, in which binary numbers are replaced with hexadecimal numbers in the brackets.

#### 1-2) Addition in $GF(2^8)$

The addition of two elements in  $GF(2^8)$  is achieved by XORing the coefficients for the corresponding powers in the polynomials (denoted by  $\oplus$ ). For two bytes  $\{a_7a_6a_5a_4a_3a_2a_1a_0\}$  and  $\{b_7b_6b_5b_4b_3b_2b_1b_0\}$ , the sum is  $\{c_7c_6c_5c_4c_3c_2c_1c_0\}$ ,

where each  $c_i = a_i \oplus b_i$ . As shown in Fig. 18, a typical adder for achieving addition in  $GF(2^8)$  includes eight XOR gates.

### 5 1-3) Multiplication in $GF(2^8)$

The multiplication in  $GF(2^8)$  corresponds with the multiplication of polynomials modulo an irreducible polynomial of degree 8. Although there are a plurality of irreducible polynomials in  $GF(2^8)$ , the AES algorithm adopts the following polynomial for defining the multiplication in  $GF(2^8)$ ;

$$m(x) = x^8 + x^4 + x^3 + x + 1. \quad \dots(2)$$

The multiplication in  $GF(2^8)$  involves the multiplication with the polynomial  $x$ , that is, a hexadecimal value {02}, in  $GF(2^8)$ , which is achieved as described below. Multiplying the binary polynomial defined in equation (1) with the polynomial  $x$  results in

$$\begin{aligned} & b_7x^8 + b_6x^7 + b_5x^6 + b_4x^5 \\ & + b_3x^4 + b_2x^3 + b_1x^2 + b_0x. \quad \dots(3) \end{aligned}$$

This operation is equivalent to a left shift by 1 bit in the binary notation.

The result of  $x \cdot b(x)$  is obtained by reducing the above result modulo  $m(x)$  defined in equation (2). If  $b_7=0$ , the result is already in reduced form. If  $b_7=1$ , the reduction is

accomplished by subtracting the polynomial  $m(x)$ , that is, XORing with  $\{00011011\}$  ( $=\{1b\}$ ) after the left shift. Fig. 19 shows a typical multiplier computing the product of an element

5  $\{b_7b_6b_5b_4b_3b_2b_1b_0\}$  with  $\{00000010\}$  ( $=\{02\}$ ).

Arbitrary multiplication in  $GF(2^8)$  can be expressed with combination of multiplication by power(s) of  $x$ , (i.e.,  $\{00000010\}$  or  $\{02\}$ ) and the addition (i.e., XORing). Fig. 20 shows a typical  
10 Galois field multiplier computing the product of two bytes  $\{a_7a_6a_5a_4a_3a_2a_1a_0\}$  and  $\{b_7b_6b_5b_4b_3b_2b_1b_0\}$  in  $GF(2^8)$ . Symbols "2x" represent the multipliers achieving multiplication by  $\{02\}$  illustrated in Fig. 19, while symbols "XOR" represent the adders  
15 illustrated in Fig. 18. As described later, encryption using the AES algorithm requires Galois field multipliers for multiplications by  $\{02\}$ , and  $\{03\}$ , while decryption using the AES algorithm requires multipliers for  
20 multiplications by  $\{09\}$ ,  $\{0b\}$ ,  $\{0d\}$ , and  $\{0e\}$ .

## 2. First Embodiment

In a first embodiment, as shown in Fig. 7, an AES encryption processor is provided with a  
25 column multiplexer 102, an input register 103, a row multiplexer 104, a S-box 105, a coefficient table 106, first to fourth Galois field

multipliers  $107_0$  to  $107_3$  (which are collectively denoted by numeral 107), an result register 108, a Galois field adder 109, and an accumulator register 110.

5           The column multiplexer 102 receives an input state 101, which is an array of 16 8-bit elements arranged in four rows and four columns. As described above, the elements of the input state 101 are denoted by  $S_{i,j}$  for  $0 \leq i, j \leq 3$ .  
10 The input state 101 may be stored in a register accessible from software in units of columns.

          The column multiplexer 102, the input register 103, and the row multiplexer 104 are responsive to column and row indices received  
15 from a controller (not shown) for selecting a requested element from the input state 101. The column multiplexer 102 selects one column, which includes four elements, from the input state 101, and provides the four elements within the  
20 selected column for the input register 103. The input register stores therein the received four elements. The row multiplexer 104 selects the requested element arranged in the requested row, and provides the selected element for the S-box  
25 105.

          The S-box 105 is used to develop an 8-bit substitution value, which is the result of the

SubBytes transformation, with the selected element used as the index. The S-box 105 is typically composed of an 8-bit 256 word ROM, RAM or a combinational circuit. As illustrated in Fig. 5 21, the values contained in the S-box 105 are identical to those disclosed in Figure 7 of FIPS 197. The substitution value, obtained using the S-box 105, is provided for the first to fourth Galois field multipliers  $107_0$  to  $107_3$ .

10           The coefficient table 106 provides 2-bit coefficients  $d_0$  to  $d_3$  for the multipliers  $107_0$  to  $107_3$  in response to the row index, which is used for selecting the requested element.

Referring to Fig. 8, the values contained 15 in the coefficient table 106 are the elements of the transposed matrix of the coefficient matrix described in equation (5.6) of FIPS 197. For the row index "0", which selects the first row of the input state 101, the coefficient table 106 sets 20 the coefficients  $d_3$ ,  $d_2$ ,  $d_1$ , and  $d_0$  to the hexadecimal numbers {02}, {01}, {01}, and {03}, respectively. For the row index "1", which selects the second row of the input state 101, the coefficient table 106 sets the coefficients  $d_3$ , 25  $d_2$ ,  $d_1$ , and  $d_0$  to the hexadecimal numbers {03}, {02}, {01}, and {01}, respectively. For the row index "2", which selects the third row of the

input state 101, the coefficient table 106 sets the coefficients  $d_3$ ,  $d_2$ ,  $d_1$ , and  $d_0$  to the hexadecimal numbers {01}, {03}, {02}, and {01}, respectively. Finally, for the row index "3",  
5 which selects the fourth row of the input state 101, the coefficient table 106 sets the coefficients  $d_3$ ,  $d_2$ ,  $d_1$ , and  $d_0$  to the hexadecimal numbers {01}, {01}, {03}, and {02}, respectively.

Referring back to Fig. 7, the Galois field  
10 multipliers 107<sub>0</sub> to 107<sub>3</sub> compute in  $GF(2^8)$  the products of the 8-bit substitution value received from the S-box 105 with the coefficients  $d_0$  to  $d_3$ , respectively. The Galois field multipliers 107<sub>0</sub> to 107<sub>3</sub> may be each composed of the multiplier  
15 illustrated in Fig. 20, with the 8-bit substitution value inputted as the bits  $b_7$  to  $b_0$ , and with the coefficient inputted as the bits  $a_1$  and  $a_0$  from the coefficient table 106. The circuit components associated with  $a_2$  to  $a_7$  may be  
20 omitted.

The result register 108 contains first to fourth bytes associated with the first to fourth rows of the output state, respectively. The products received from the multipliers 107<sub>0</sub> to  
25 107<sub>3</sub> are stored as the first to fourth data bytes in the result register 108, respectively. The output of the result register 108 is connected to

'the' Galois field adder 109.

The Galois field adder 109 and the accumulation register 110 are used to accumulate the products obtained by the Galois field multipliers 107<sub>0</sub> to 107<sub>3</sub> for the first to fourth rows of the output state. The Galois field adder 109 computes the sums of the corresponding bytes received from the result register 108 and the accumulator register 110. The accumulation register 110 latches the computed sums received from the Galois field adder 109. After the SubBytes, ShiftRows, and MixColumns transformations for a desired column are completed, the four elements of the desired column of the output state are developed in the accumulation register 110.

It should be noted that the input register 103 and the result register 108 are provided for pipeline processing. Therefore, the input register 103 and the result register 108 should not be understood as being essential for the AES encryption processor.

Fig. 9 illustrates the procedure implemented by the AES encryption processor in this embodiment for obtaining the first column of the output state, that is, the resultant state obtained through the SubBytes, ShiftRows, and

MixColumns transformations. The  $(i, j)$  element of the output state is referred to as  $S'_{i,j}$ , hereinafter.

The procedure begins with resetting the accumulator register 110 at Step S301. Resetting the accumulator register 110 is followed by implementing transformations for the  $(0, 0)$  element  $S_{0,0}$  of the input state 101. In response to the column index being set to "0", the column multiplexer 102 selects the first column of the input state 101 at Step S302. Correspondingly, the row multiplexer 104 selects the first row of the input state 101 at Step S303. This results in that the row multiplexer 104 outputs the  $(0, 0)$  element  $S_{0,0}$  of the input state 101.

The substitution transformation using the S-box 105 is then implemented to develop the substitution value  $S''_{0,0}$  with the element  $S_{0,0}$  used as the index at Step S304.

The coefficient table 106 provides four coefficients  $d_0$  to  $d_3$  in response to the row index being set to "0". As described below, the coefficients  $d_0$ ,  $d_1$ ,  $d_2$ , and  $d_3$  are respectively used for obtaining the  $S'_{0,j}$ ,  $S'_{1,j}$ ,  $S'_{2,j}$ , and  $S'_{3,j}$  elements of the output state.

The multipliers 107<sub>0</sub> to 107<sub>3</sub> then computes the products of the substitution value  $S''_{0,0}$  with



the four coefficients  $d_0$  to  $d_3$ , received from the coefficient table 106, respectively, the products being denoted by ' $S_{0,0} \cdot \{02\}$ ', ' $S_{0,0} \cdot \{01\}$ ', ' $S_{0,0} \cdot \{01\}$ ', and ' $S_{0,0} \cdot \{03\}$ '.

5           The multipliers  $107_0$  to  $107_3$  provide the products as the four output bytes for the Galois field adder 109 at Step S305. The adder 109 computes the sums of the corresponding bytes received from the multipliers  $107_0$  to  $107_3$ , and the  
10 accumulator register 110. The four bytes stored in the accumulator register 110 are respectively updated to the sums of the corresponding bytes at Step S306.

Correspondingly, the elements  $S_{1,1}$ ,  $S_{2,2}$ , and  
15  $S_{3,3}$  are then processed successively. The elements  $S_{1,1}$ ,  $S_{2,2}$ , and  $S_{3,3}$  are serially selected by the column and row multiplexers 102 and 104, and the substitution values  $S_{1,1}$ ,  $S_{2,2}$ , and  $S_{3,3}$  are successively obtained using the S-box 105 for the  
20 elements  $S_{1,1}$ ,  $S_{2,2}$ , and  $S_{3,3}$ . The substitution values  $S_{1,1}$ ,  $S_{2,2}$ , and  $S_{3,3}$  are each multiplied with the coefficients  $d_0$  to  $d_3$ . The sums of the corresponding bytes received from the multipliers  $107_0$  to  $107_3$  and the accumulator register 110 are  
25 then successively computed by the Galois field adder 109 for each of the substitution values  $S_{1,1}$ ,  $S_{2,2}$ , and  $S_{3,3}$  to update the stored bytes

within the accumulator register 110. The completion of the addition by the Galois field adder 109 for the element  $S_{3,3}$  results in that the four elements  $S'_{0,0}$ ,  $S'_{1,0}$ ,  $S'_{2,0}$ , and  $S'_{3,0}$ , of the first column of the output state are developed in the accumulator register 110. This process is equivalent to implementing the SubBytes, ShiftRows, and MixColumns transformations for obtaining the first column of the output state.

10           The same goes for the remainder columns of the output state. The second column of the output state is obtained from the elements  $S_{0,1}$ ,  $S_{1,2}$ ,  $S_{2,3}$ , and  $S_{3,0}$ , the third column from the elements  $S_{0,2}$ ,  $S_{1,3}$ ,  $S_{2,0}$ , and  $S_{3,1}$ , and the fourth column is  
15 obtained from the elements  $S_{0,3}$ ,  $S_{1,0}$ ,  $S_{2,1}$ , and  $S_{3,2}$ .

          The architecture in this embodiment effectively reduces necessary hardware while achieving the parallel processing. The coefficient table 106, the multipliers 107<sub>0</sub> to  
20 107<sub>4</sub>, and the adder 109 eliminate the need for preparing a plurality of S-boxes (or expanded S-boxes) for implementing parallel processing in connection with a single column of the output state.

25           For instance, the architecture in this architecture typically requires about one sixteenth of hardware compared to that of the

1 'aforementioned Gladman's method. The Gladman's  
method requires four lookup tables; each contains  
256 32-bit words, that is, a 32k-bit memory. In  
contrast, the architecture in this architecture  
5 requires the single S-box 105 containing 256 8-  
bit words, that is, a 2k-bit memory. Because the  
hardware sizes of the Galois field multipliers  
107 are negligible, the required hardware can be  
considered as being proportional to the hardware  
10 size of S-boxes (or expanded S-box). This deduces  
that the architecture in this architecture  
effectively reduces hardware compared to the  
Gladman's method.

15 3. Second Embodiment

In a second embodiment, as illustrated in  
Fig. 10, an AES encryption processor is provided  
which is adapted to an instruction set including  
an AES-dedicated instruction denoted by "AES\_SSM",  
20 which requests the SubBytes, ShiftRows, and  
MixColumns transformations. The following is the  
mnemonic code for the AES\_SSM instruction:

AES\_SSM rs, rt, imm,

where the operand rs indicates an input register,  
25 the operand rt indicates an output register, and  
the operand imm is an immediate operand  
indicating a row index used for selecting the row

of the desired element.

Figs. 11A and 11B illustrate the data to be stored in the input and output registers *rs* and *rt*. The registers *rs* and *rt* are adapted to contain four-byte data, which allows the registers *rs* and *rt* to store therein four elements of a desired column of a state. The four bytes stored in the input register *rs* are denoted by symbols *bi0* to *bi3*, while the four bytes stored in the output register *rt* are denoted by symbols *bo0* to *bo3*. The bytes *bi0* to *bi3* are respectively associated with the first to fourth rows of the input state. Correspondingly, the bytes *bo0* to *bo3* are respectively associated with the first to fourth rows of the output state.

Referring back to Fig. 10, the AES encryption processor includes a register file 401 including general-purpose registers *r1* to *rn*, an instructions buffer 402, a decoder 403, auxiliary registers 403 to 409, an arithmetic logic unit (ALU) 410, a result register 411, a write multiplexer 412, a row multiplexer 104, a S-box 105, a coefficient table 106, Galois field multipliers  $107_0$  to  $107_3$ , and a result register 108, where the Galois field multipliers  $107_0$  to  $107_3$  are collectively denoted by numeral 107. In response to the operands of the AES\_SSM

instruction, one of the general-purpose registers is selected as the input register *rs*, another is selected as the output register *rt*.

Circuitry 111' surrounded with a broken line in Fig. 10 functionally corresponds with the circuitry 111 in Fig. 7. Therefore, detailed description of the circuitry 111' is not given.

The auxiliary registers 408 and 409 receive four-byte data from selected two of the general-purpose registers within the register file 401.

The ALU 410 is used for XORing the four-byte data stored in the auxiliary registers 408 and 409. The result of the XORing is transferred to the result register 411.

The write multiplexer 412 selects one of the four-byte data received from the result registers 108 and 411. The selected data is stored in one of the general-purpose registers within the register file 401, which is selected as the output register *rt*.

It should be noted that the auxiliary registers 404 to 409 and the result registers 108 and 411 are provided for pipeline processing. Therefore, these registers should not be understood as being essential for the AES encryption processor.

Fig. 12 illustrates the result of an

'AES\_SSM instruction developed in the output register rt, which is selected by the operand rt. An input state is stored into selected four registers within the register file 401; each of the four registers stores therein four elements of the corresponding column of the input state. The operand rs selects one of the registers of the register file 401, that is, one of the columns of the input state. The operand imm is used as the row index that selects one of the rows of the input state. In other words, the operands rs and imm are used to select one of the 16 elements of the input state.

When the operand imm of the AES\_SSM instruction is set to a value "00", which selects the first row of the input state, the issue of the AES\_SSM instruction results in that the bytes bo0 to bo3 are set to S-box(bi0)•{02}, S-box(bi0)•{01}, S-box(bi0)•{01}, and S-box(bi0)•{03}, respectively, where S-box(bik) represents the substitution value obtained using the S-box 105 with the byte bik within the input register rs used as the index. Correspondingly, the result of the AES\_SSM instruction is obtained as illustrated in Fig. 12 for other rows.

In detail, the result of the AES\_SSM instruction is obtained as described below.

Referring back to Fig. 10, when an AES\_SSM instruction is issued, the AES\_SSM instruction is latched by the instruction buffer 402 and decoded by the decoder 403. The decoder 403 obtains the  
5 operands rs, rt, and imm from the instruction. The obtained operand imm is transferred to the auxiliary register 405.

In response to the operand rs, which selects one of the columns of the input state,  
10 one of the registers within the register file 401 is selected as the input register rs, and the four bytes stored in the input register rs is then transferred to the row multiplexer 104. It should be noted that the four bytes corresponds  
15 with the four elements of the selected column of the input state.

The row multiplexer 104 selects one of the transferred four bytes, and the selected byte is stored in the auxiliary register 404. It should  
20 be noted that the selected byte corresponds with the selected element.

In response to the selected byte received from the auxiliary register, the substitution value is obtained using the S-box 105 with the  
25 selected byte used as the index. The obtained substitution value is then latched by the auxiliary register 407.

The coefficient table 106 is responsive to the operand imm received from the auxiliary register 405, which is used as the row index, to provide a set of coefficients  $d_0$  to  $d_3$  for the  
5 auxiliary register 406.

The Galois field multiplexers  $107_0$  to  $107_3$ , respectively receive the coefficients  $d_0$  to  $d_3$  from the auxiliary register 406, and compute the products of the selected byte (or element) with  
10 the corresponding coefficients. The computed products constitute resultant four-byte data, and the four-byte data is stored in the result register 408. The four-byte data stored in the result register 408 is selected by the write  
15 multiplexer 412 and transferred to the output register rt, which is selected from among the registers within the register file 401 by the operand rt received from the decoder 403.

The use of the AES\_SSM instruction  
20 effectively facilitates the SubBytes, ShiftRows, and MixColumns transformations during encryption. Fig. 13 illustrates an exemplary sequence of instructions for performing the SubBytes, ShiftRows, and MixColumns transformations for  
25 obtaining the first column of the output state.

Performing the SubBytes, ShiftRows, and MixColumns transformations begins with initially



storing the input state into selected four registers within the register file 401. In this embodiment, the elements  $S_{3,3}$ ,  $S_{2,3}$ ,  $S_{1,3}$ , and  $S_{0,3}$  of the input state are stored in the register r3, 5 and the elements  $S_{3,2}$ ,  $S_{2,2}$ ,  $S_{1,2}$ , and  $S_{0,2}$  are stored in the register r2. Correspondingly, the elements  $S_{3,1}$ ,  $S_{2,1}$ ,  $S_{1,1}$ , and  $S_{0,1}$  are stored in the register r1, and the elements  $S_{3,0}$ ,  $S_{2,0}$ ,  $S_{1,0}$ , and  $S_{0,0}$  are stored in the register r0. It should be 10 noted that the elements  $S_{k,1}$  are stored as the bytes bik in the registers r0 to r3.

The SubBytes, ShiftRows, and MixColumns transformations are achieved by seven instructions: four AES\_SSM instructions, and 15 three XOR instructions, where the XOR instruction designates an instruction attached with first to three operands which performs XORing the values stored in the registers indicated by the first and second operands thereof in  $GF(2^8)$ , and storing 20 the result in the register indicated by the third operand.

The XOR instruction is performed as described in the following. As is the case of the AES\_SSM instructions, upon being issued, the XOR 25 instruction is latched by the instruction buffer 402, and decoded by the decoder 403. In response to the operands of the XOR instruction, two four-

'byte' data are obtained from selected two registers within the register file 401, and each stored in the auxiliary registers 408 and 409. The ALU 410 performs XORing the two four-byte data received from the auxiliary registers 408 and 409, that is, achieves the addition of the corresponding bytes in  $GF(2^8)$ . The resultant four-byte data obtained by the XORing is stored in the result register 411. The resultant four-byte data is selected by the write multiplexer 412, and stored in the output register indicated by the third operand.

The sequence of the instructions presented in Fig. 13 achieves data processing equivalent to that performed by the processor illustrated in Fig. 7. It should be noted that selecting the input register  $rs$  is equivalent to selecting the target column with the column index, and performing the XOR instructions is equivalent to achieving the addition in  $GF(2^8)$  by the Galois field adder 109.

The use of the aforementioned AES\_SSM instructions effectively reduces the number of necessary instructions for achieving encryption using the AES algorithm. As described above, performing the SubBytes, ShiftRows, and MixColumns transformations for obtaining one

column of the output state requires only seven instructions, that is, obtaining the output state requires 28 instructions. This results in that performing ten rounds, which are required to encryption with 128-bit key, requires about 300 instructions including performing the AddRoundKey transformations. The reduction of the number of the required instructions effectively achieves processing speed at least as good as the Gladman's method with reduced hardware for storing the S-box.

#### 4. Modification for performing decryption

Minor modifications allow the AES processors in the first and second embodiments to perform decryption with the AES algorithm in place of encryption. First, the values contained in the coefficient table 106 are replaced with the 4-bit elements of the transposed matrix of the coefficient matrix described in equation (5.10) of FIPS 197 as illustrated in Fig. 14. For the row index "0" (or the operand imm being "00"), which selects the first row of the input state 101, the coefficient table 106 sets the coefficients  $d_3$ ,  $d_2$ ,  $d_1$ , and  $d_0$  to the hexadecimal numbers {0e}, {09}, {0d}, and {0b}, respectively. For the row index "1", which selects the second

row" of the input state 101, the coefficient table 106 sets the coefficients  $d_3$ ,  $d_2$ ,  $d_1$ , and  $d_0$  to the hexadecimal numbers {0b}, {0e}, {09}, and {0d}, respectively. For the row index "2", which  
5 selects the third row of the input state 101, the coefficient table 106 sets the coefficients  $d_3$ ,  $d_2$ ,  $d_1$ , and  $d_0$  to the hexadecimal numbers {0d}, {0b}, {0e}, and {09}, respectively. Finally, for the row index "3", which selects the fourth row of  
10 the input state 101, the coefficient table 106 sets the coefficients  $d_3$ ,  $d_2$ ,  $d_1$ , and  $d_0$  to the hexadecimal numbers {09}, {0d}, {0b}, and {0e}, respectively.

Second, the S-box 105 is replaced with an  
15 inverse S-box illustrated in Fig. 22, as disclosed in Figure 14 of FIPS 197.

These modifications requires the Galois field multipliers 107<sub>0</sub> to 107<sub>3</sub> to be adapted to achieve multiplication of the 8-bit substitution  
20 values with the 4-bit coefficients in  $GF(2^8)$ .

An inverse AES\_SSM instruction may be defined for the AES processor in Fig. 10 in place of the AES\_SSM instruction in the case that the values of the coefficient table 106 are modified  
25 and the S-box 105 is replaced with the inverse S-box table.

Fig. 15 illustrates the result of an

inverse AES\_SSM instruction developed in the  
output register rt. When the operand imm of the  
inverse AES\_SSM instruction is set to a value  
"00", which selects the first row of the input  
5 state, the issue of the inverse AES\_SSM  
instruction results in that the bytes bo0 to bo3  
are set to  $\text{InvS-box}(bi0) \cdot \{0e\}$ ,  $\text{InvS-box}(bi0) \cdot \{09\}$ ,  
 $\text{InvS-box}(bi0) \cdot \{0d\}$ , and  $\text{InvS-box}(bi0) \cdot \{0b\}$ ,  
respectively, where  $\text{InvS-box}(bik)$  represents the  
10 substitution value obtained using the inverse S-  
box with the byte bik within the input register  
rs used as the index. Correspondingly, the result  
of the inverse AES\_SSM instruction is obtained as  
illustrated in Fig. 15 for other rows.

15

### 5. Third Embodiment

Referring to Fig. 16, in a third embodiment,  
an AES processor is provided which is adapted to  
both encryption and decryption using the AES  
20 algorithm. This is achieved by replacing the  
circuitry 111' illustrated in Fig. 10 with the  
circuitry illustrated in Fig. 16. The AES  
processor in this embodiment is designed on the  
basis of the fact that there is no significant  
25 difference between encryption and decryption  
using the AES algorithm.

Referring to Fig. 16, the AES processor in

this embodiment includes an inverse affine transformation circuit 1101, an encryption multiplexer 1102, an inverse table 1103, an affine transformation circuit 1104, an encryption  
 5 multiplexer 1105, a row multiplexer 104, a coefficient table 106, Galois field multiplexers 107, and a result register 108.

The row multiplexer 104 receives the four elements of the selected column of the input  
 10 state 101, and selects one of the four elements.

The encryption multiplexer 1102 selects one of the outputs received from the inverse affine transformation circuit 1101 and the row multiplexer 104, while the encryption multiplexer  
 15 1105 selects one of the outputs received from the inverse table 1103 and the affine transformation circuit 1104.

The affine transformation circuit 1104 applies the following affine transformation over  
 20  $GF(2^8)$ :

$$b'_i = b_i \oplus b_{(i+4) \bmod 8} \oplus b_{(i+5) \bmod 8} \oplus b_{(i+6) \bmod 8} \\ \oplus b_{(i+7) \bmod 8} \oplus c_i, \quad \dots (4)$$

for  $0 \leq i \leq 7$ , where  $b_i$  is the  $i^{\text{th}}$  bit of the input byte,  $c_i$  is the  $i^{\text{th}}$  bit of a byte  $c$  with the value  
 25 {63}, and  $b'_i$  is the  $i^{\text{th}}$  bit of the output byte.

The inverse affine transformation circuit 1101, on the other hand, applies the following

inverse affine transformation over  $GF(2^8)$ :

$$b'_i = b_{(i+2) \bmod 8} \oplus b_{(i+5) \bmod 8} \oplus b_{(i+7) \bmod 8} \oplus c_i, \quad \dots (5)$$

for  $0 \leq i \leq 7$ , where  $b_i$  is the  $i^{\text{th}}$  bit of the input byte,  $c_i$  is the  $i^{\text{th}}$  bit of a byte  $c$  with the value {05}, and  $b'_i$  is the  $i^{\text{th}}$  bit of the output byte.

The inverse table 1103 is used for taking the multiplicative inverse in  $GF(2^8)$ . Fig. 23 shows the values contained in the inverse table 1103. A table lookup using the inverse table 1103 with the input byte {xy} used as the index provides the multiplicative inverse of the input byte {xy} in  $GF(2^8)$ .

The table lookup on the S-box 105 for encryption is equivalently achieved by the table lookup on the inverse table 1103 followed by applying the aforementioned affine transformation with the affine transformation circuit 1104. As described in FIPS 197, Section 5.1.1, the SubBytes transformation is constructed by taking the multiplicative inverse in  $GF(2^8)$  followed by applying the aforementioned affine transformation.

Correspondingly, the table lookup on the inverse S-box for decryption is equivalently achieved by applying the aforementioned inverse affine transformation with the inverse affine transformation circuit 1101 followed by the table

lookup on the inverse table 1103.

In this embodiment, encryption and decryption are performed in response to an issue of an AES instruction that includes an operator, a first operand indicating the input register, a second operand indicating the output register, and an immediate operand indicating the row of the input state. The immediate operand additionally includes a bit for selecting one of encryption and decryption operations.

When the encryption operation is selected by the selecting bit, the encryption multiplexer 1102 selects the output of the row multiplexer 104, and the encryption multiplexer 1105 selects the output of the affine transformation circuit 1104. The multiplicative inverse of the selected element received from the row multiplexer 104 is obtained using the inverse table 1103, and the aforementioned affine transformation operates on the obtained multiplicative inverse. This results in that the substitution using the S-box 105 is equivalently implemented on the selected element. In addition, in response to the encryption operation being selected by the selecting bit, the coefficient table 106 provides a set of coefficients  $d_0$  to  $d_3$  as illustrated in Fig. 8, and the multiplication in  $GF(2^8)$  is achieved by



the Galois field multipliers 107. The products computed by the Galois field multipliers 107 are used for obtaining the four elements of the desired column of the output state.

5           When the decryption operation is selected by the selecting bit, on the other hand, the encryption multiplexer 1102 selects the output of the inverse affine transformation circuit 1101, , and the encryption multiplexer 1105 selects the  
10 output of the inverse table 1103. The aforementioned inverse affine transformation operates on the selected element received from the row multiplexer, and the multiplicative inverse of the result of the inverse affine  
15 transformation is obtained using the inverse table 1103. This results in that the substitution using the inverse S-box is equivalently implemented on the selected element. In addition, in response to the decryption operation being  
20 selected by the selecting bit, the coefficient table 106 provides a set of coefficients  $d_0$  to  $d_3$ , as illustrated in Fig. 14, and the multiplication in  $GF(2^8)$  is achieved by the Galois field multipliers 107. The products computed by the  
25 Galois field multipliers 107 are used for obtaining the four elements of the desired column of the output state.

The architecture in this embodiment advantageously eliminates a need for including both the S-box and inverse S-box for performing both encryption and decryption; instead, the architecture requires only the inverse table 1103 for performing the SubBytes and InvSubBytes transformations. This effectively reduces hardware of the AES processor.

#### 10 6. Fourth Embodiment

In a fourth embodiment, as shown in Fig. 17, AES processor cores are multiplexed in an AES processor to achieve parallel processing. This is achieved by replacing the circuitry 111' illustrated in Fig. 10 with the circuitry illustrated in Fig. 17.

In detail, the circuitry illustrated in Fig. 17 includes AES processor cores 1202 and 1203, and a coefficient table 106. A 64-bit (8-byte) input register 1201 and a 64-bit (8-byte) output register 1204 is selected out of the register file in response to the operand rs and rt of the AES instruction. The AES processor cores 1202 and 1203 has the same structure as the circuitry illustrated in Fig. 16 with exception of the coefficient table 106, which are shared by the AES processor cores 1202 and 1203.

The input register 1201 is used for storing two columns to be processed; the two columns may be retrieved from a single input state or from a pair of different input state. The upper four  
5 bytes of the input register 1201 are provided for the AES processor core 1202, while the lower four bytes are provided for the AES processor core 1203.

The AES processor cores 1202 and 1203  
10 implements the operations in response to the immediate operand of the AES instruction as described in the third embodiment. The immediate operand selects the row to be operated and the additional selecting bit within the immediate  
15 operand selects one of the encryption and decryption operations.

The output register 1204 receives the outputs from the AES processor cores 1202 and 1203. The output received from the AES processor  
20 core 1202 is stored as the upper four bytes within the output register 1204, while the output received from the AES processor core 1203 is stored as the lower four bytes.

In this embodiment, the AES processor cores  
25 are multiplexed within the AES processor, and this effectively improves processing speed.

It should be noted that an additional AES

processor core(s) may be prepared for the AES processor in the case that the bit width of the input and output registers 1201 and 1204 are larger than 64.

5

## 7. Conclusion

As thus described, the architecture including the coefficient table 106 and the Galois field multipliers 107 eliminates a need  
10 for providing a plurality of S-boxes (or inverse S-boxes) to achieve parallel processing. This effectively achieves reduction of required hardware with improved efficiency.

In addition, the use of the inverse table  
15 with the affine and inverse affine transformation circuits advantageously reduces required hardware more effectively.

Although the invention has been described in its preferred form with a certain degree of particularity, it is understood that the present  
20 disclosure of the preferred form has been changed in the details of construction and the combination and arrangement of parts may be resorted to without departing from the scope of  
25 the invention as hereinafter claimed.

For example, the details of the instruction set may be modified. The row to be operated may

be selected the operator itself. That is, four different instructions associated with different rows are provided in place of the AES\_SSM instruction. The same goes for the inverse  
5 AES\_SSM instruction described in Section 4, and the AES instruction described in Section 5.

The input or output states may be stored in a memory in place of the register file. In this case, the operand of the instruction indicates  
10 the address of the memory in place of selecting the register.